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Cation Dynamics in Hybrid Halide Perovskites

Eve M. Mozur and James R. Neilson

Department of Chemistry, Colorado State University, Fort Collins, Colorado 80523, USA;
email: jrn@colostate.edu

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Abstract

Hybrid halide perovskite semiconductors exhibit complex, dynamical disorder while also harboring properties ideal for optoelectronic applications that include photovoltaics. However, these materials are structurally and compositionally distinct from traditional compound semiconductors composed of tetrahedrally coordinated elements with an average valence electron count of silicon. The additional dynamic degrees of freedom of hybrid halide perovskites underlie many of their potentially transformative physical properties. Neutron scattering and spectroscopy studies of the atomic dynamics of these materials have yielded significant insights into their functional properties. Specifically, inelastic neutron scattering has been used to elucidate the phonon band structure, and quasi-elastic neutron scattering has revealed the nature of the uncorrelated dynamics pertaining to molecular reorientations. Understanding the dynamics of these complex semiconductors has elucidated the temperature-dependent phase stability and origins of defect-tolerant electronic transport from the highly polarizable dielectric response. Furthermore, the dynamic degrees of freedom of the hybrid perovskites provide additional opportunities for application engineering and innovation.

1. INTRODUCTION: HYBRID HALIDE PEROVSKITE SEMICONDUCTORS

Hybrid halide perovskites and their structural derivatives have advantageous optoelectronic properties for a relatively wide range of applications. The tunable bandgap, defect tolerance, and long electronic excited-state lifetimes of these perovskites make them ideal semiconductors for photovoltaics (1, 2). The heavy elements in these materials also allow their use in X-ray and γ-ray detection (3, 4). Changing the composition or reducing the effective dimensionality changes the electronic structure and exciton binding energy to increase the efficiency of light emission; several materials even reemit white light intrinsically (5). This family of materials provides new opportunities for building the structure–property relationships of next-generation semiconductors.

Hybrid halide perovskites exhibit additional dynamic degrees of freedom in comparison to traditional compound semiconductors (e.g., CdTe, GaAs, TlBr). Materials such as $(CH_3NH_3)PbI_3$ and $(CH(NH_2)_2)PbI_3$ are plastic crystals, as schematically depicted in **Figure 1a**: The organic cations exhibit translational symmetry with respect to their center of mass but without orientational order (7). The molecular sphere approximated by rotating the molecules can be used to compute a revised Goldschmidt tolerance factor based on the ionic radii of the constituent ions (8) (**Figure 1b**), which is often employed to predict the formation of a crystal structure analogous to the mineral perovskite $CaTiO_3$ (9). Similar to oxide perovskites, halide perovskites typically undergo phase transitions on cooling, as characterized by a reduction in symmetry from cubic to tetragonal to orthorhombic that is related to cooperative tilting of the octahedral framework (10, 11). However, the rich and subtle details of these transitions and the resulting properties of each phase cannot be fully understood without considering the plastic crystalline nature of these materials (12).

Various advantageous electronic properties in hybrid perovskites have been attributed to their dynamic, plastic crystalline behavior. While long electronic excited-state lifetimes have been linked to collective dynamics of the extended octahedral framework (i.e., phonons) (13–17), such long-lived excited states are also linked to organic cation reorientational dynamics by way of giant polaron (18), phonon bottleneck (19, 20), or Rashba splitting–based (21) mechanisms
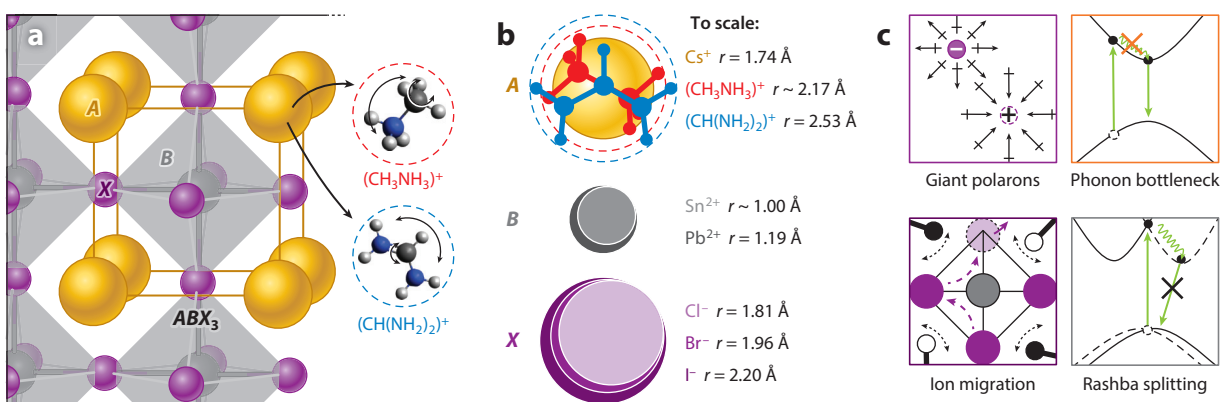
Figure 1

(*a*) Schematic illustration of the plastic crystalline nature of hybrid perovskites of the formula *ABX*$_3$, as well as the principal rotations of methylammonium, $(CH_3NH_3)^+$, and formamidinium, $(CH(NH_2)_2)^+$. (*b*) Diagram illustrating the scale of the various ions found in hybrid halide perovskites on the basis of their Shannon–Prewitt radii (6) or estimated molecular size (8). (*c*) Commonly proposed electron–phonon interactions in hybrid halide perovskites involving organic cation dynamics.

(described in more detail in Section 2.2.2) (**Figure 1c**). Furthermore, the presence of an organic cation has been associated with the so-called self-healing of photoinduced defects (22) and aids in photoinduced ionic conductivity (23–25). The ionic mobility of hybrid halide perovskites is often linked to decomposition (26–29) and is hypothesized to relate to stationary atomic fluctuations (30), akin to the paddlewheel mechanism in materials studied for alkali ion conduction (31, 32). Similar dynamics are thought to influence relaxation pathways in layered perovskite derivatives of interest as phosphors (33, 34); the microscopic details remain an active area of research. Regardless of the proposed mechanism, the impressive defect-tolerant properties of hybrid halide perovskites advance high-efficiency photovoltaics (1, 35, 36). This review focuses on how neutron scattering (described in the sidebar titled Neutron Scattering: A Brief Primer), particularly quasi-elastic neutron scattering (QENS, described in the sidebar titled Quasi-Elastic Neutron Scattering: A Closer Look), has addressed questions related to these properties by characterizing the dynamic nature of organic cations in hybrid perovskite semiconductors.

Incoherent scattering: yields information independent of positional correlations

NEUTRON SCATTERING: A BRIEF PRIMER

Neutron scattering is a powerful tool to investigate the structure and dynamics of materials through analysis of the dynamic structure factor, $S(Q, \omega)$ (**Figure 2a**). The large large momentum of neutrons (relative to X-rays) allows them to couple strongly to atomic and molecular dynamics. The scattering cross section depends on interactions of the neutron with the nuclei within each atom and is therefore isotope dependent (37) (**Figure 2b**) and provides complementary atomic contrast to X-ray scattering techniques that depend on the square of the atomic number. Therefore, short wavelengths (0.5–4 Å) are suitable for diffraction, while their energies (μeV–eV) are ideal for spectroscopy. The neutron scattering techniques most relevant for investigating the structure and dynamics of materials include neutron diffraction, quasi-elastic neutron scattering (QENS), and inelastic neutron scattering (INS), as summarized in **Figure 2**. INS probes the vibrational density of states between ~5 and 1,000 meV. QENS probes dynamics on the μeV energy scale, encompassing molecular reorientations, translations, and diffusion. These dynamics map onto the dielectric response function illustrated in **Figure 2e,f**.

QENS is complementary to other techniques sensitive to motions on 10^{-9}–10^{-12} s timescales, such as nuclear magnetic and optical spectroscopies [e.g., Brillouin light scattering (38) or ultrafast spectroscopy (39)].

QUASI-ELASTIC NEUTRON SCATTERING: A CLOSER LOOK

QENS is performed on neutron spectrometers with excellent energy resolution ($\Delta E \sim 1$–3 μeV) and yields information about slow motions corresponding to relaxation of nearly stationary states, such as diffusion or molecular relaxation via translations or rotations. These relaxations provide a Doppler broadening of the elastic scattering as a result of the small energy transfer between neutrons and the moving nuclei in the sample.

To analyze the molecular motions, one can use a jump model, as molecules are assumed to reside in preferred orientations with jumps between well-defined orientations (40). The quasi-elastic line width relates to the timescale of this residence time between jumps (Lorentzian half-width at half-maximum $= \hbar/\tau$) (**Figure 2a**). When analyzing purely incoherent scattering, the elastic incoherent structure factor (EISF), which equals $I_{elastic}/(I_{elastic} + I_{quasi\text{-}elastic})$, can be fitted with the jump model to extract the type of motion, including the local symmetry of motion, distance of motion, and geometry of the moving object, as illustrated in **Figure 2c**.

Incoherent elastic scattering yields information about thermal motion, which follows a Q-dependent attenuation depending on the mean squared displacement (MSD) of atomic motion via the Debye–Waller factor, $\exp(-q^2 \langle u^2 \rangle /3)$, for isotropic, harmonic motion, as shown in **Figure 2d**.

2. BACKGROUND: DYNAMICS AND ELECTRONIC PROPERTIES

The frontier electronic states of halide perovskites couple primarily to low-energy optical phonons. The influence of lattice dynamics on semiconductors typically revolves around a discussion of the scattering of charge carriers from electron–phonon coupling. In compound semiconductors with diamond-type structure, such as GaAs, optical phonons reside near ~40 meV; thus, they are not appreciably populated at room temperature and play a relatively small role in electron–phonon scattering processes (45). In contrast, halide perovskite optical phonons reside between ~5 and ~12 meV (**Figure 2**). Therefore, a complete understanding of the charge transport necessitates characterization of the electron–phonon coupling. In this section, we provide a brief overview of the importance of these collective dynamics in the context of light-absorbing hybrid semiconductors for photovoltaics, and then we discuss the presence and role of localized (i.e., aperiodic) dynamics and their proposed roles in influencing the optoelectronic performance of hybrid perovskites and related semiconductors.

2.1. Collective, Periodic Dynamics: Phonons

Optical phonons, derived primarily from the cooperative dynamics within the octahedral frame-work, drive the phase behavior of halide perovskites. Akin to the ferroelectric perovskite oxides
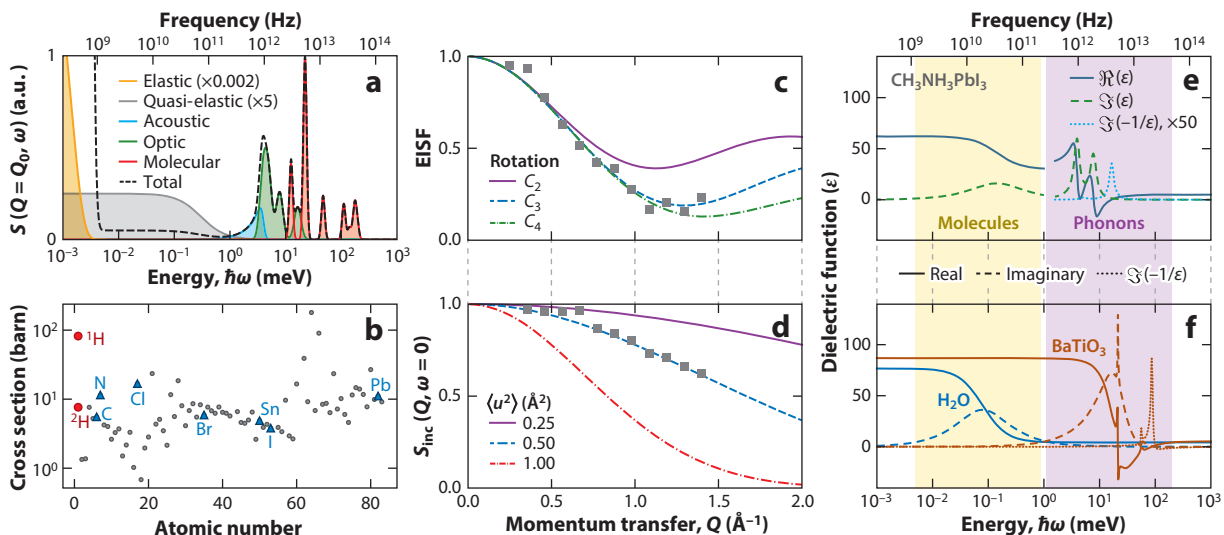

Figure 2

(*a*) Schematic representation of features observable in neutron spectroscopy, including elastic scattering from static atoms, quasi-elastic neutron scattering (QENS) from molecular reorientational dynamics, and inelastic neutron scattering from quantized lattice vibrations (acoustic and optical phonons) and molecular vibrations. (*b*) Neutron scattering cross section of different natural abundance–averaged elements (37), highlighting the large cross section of ^{1}H relative to the other elements germane to hybrid perovskites. (*c*) The elastic incoherent structure factor (EISF) used to extract details of molecular motion from momentum transfer dependence of the QENS, illustrated by three different jump models corresponding to C_2, C_3, and C_4 rotations of the same hypothetical molecule. Gray squares represent hypothetical data at discrete values of Q from one sample at fixed temperature. Different jump models can be challenging to discriminate without a sufficient Q range. (*d*) Schematic illustration of incoherent elastic scattering as a function of momentum transfer, $S_{inc}(Q, \omega = 0)$, used to extract the neutron scattering cross-section-weighted atomic mean squared displacement, $\langle u^2 \rangle = 0.5$ Å^2. Gray squares represent hypothetical data at discrete values of Q from one sample at fixed temperature. (*e*,*f*) Dielectric function, ε, including the real (*solid line*), imaginary (*dashed line*), and $\Im(-1/\varepsilon)$ (*dotted line*) components of (*e*) $CH_3NH_3PbI_3$ (41, 42) at 298 K versus (*f*) molecular, liquid H_2O at 298 K (43) and paraelectric ceramic $BaTiO_3$ at 1,000 K (44). The frequency-dependent dielectric function highlights contributions from either molecules (*beige*) or phonons (*lavender*), as detectable by neutron scattering (panel *a*).

with symmetry-lowering phase transitions on cooling from a paraelectric phase (46), the phonons related to these phase transitions contribute a significant dielectric response, as in the case of $BaTiO_3$ (**Figure 2f**). Perovskite halides undergo similar symmetry-lowering phase transitions involving changes to the octahedral tilting upon cooling, which relate to soft phonon modes (47–49). Significant entropy releases accompany these canonical phase transitions (50), related to the loss of orientational degrees of freedom of the organic molecule within the changing shape of the nominally cuboctahedral A-site void (51–54).

These same collective dynamics influence charge transport primarily through electron–phonon coupling. The optical phonons generate just over half of the polarizability in the dielectric response of $CH_3NH_3PbI_3$, as shown in **Figure 2e**. In halide perovskites, electron–phonon scattering via the Fröhlich interaction (55) limits the mobility of both free carriers and excitons; therefore, the Fröhlich interaction is the most important form of electron–phonon coupling (14–16). The magnitude of the Fröhlich interaction in $CH_3NH_3PbI_3$ [$\alpha = 1.7$–2.4 (18)] derives predominantly from an $\sim$11-meV longitudinal optic phonon (**Figure 2e**) and compares with that of other halide semiconductors, such as TlBr ($\alpha = 2.05$). This value contrasts with the smaller coupling constants of diamond-lattice, tetrahedral semiconductors GaAs ($\alpha = 0.068$) and CdTe ($\alpha = 0.39$) (17, 42).

2.2. Independent, Aperiodic Dynamics

In addition to collective motions quantized as phonons, hybrid halide perovskites exhibit more localized, aperiodic motions of both the metal–halide framework and the organic molecules.

2.2.1. Inorganic dipolar dynamics. The fluctuations of lone-pair electrons (56) modify the structure and properties of hybrid perovskites. They have been linked to many exciting aspects of hybrid perovskites, including the large ionic dielectric responses, light holes, and unconventional bandgap: All contribute to the favorable electronic transport and defect tolerance (57). The behavior of these inorganic dipoles (58) resembles that of plastic crystals with permanent, molecular dipoles [e.g., potassium cyanide (7, 59, 60)], but with dynamics on a fast 10^{14}-Hz timescale rather than the slower $\sim$$10^{12}$-Hz timescale that is associated with the ionic dynamics shown in **Figure 2e,f**.

All-inorganic perovskites exhibit significant polar dynamics from anharmonic ionic fluctuations, attributed to a head-to-head motion of cesium ions (61). Such polar fluctuations and deformations of the $[BX_6]$ octahedra have been implicated in the formation of polarons, which screen excited-state charge carriers that increase the excited-state lifetimes (62, 63). This explains how all inorganic halide perovskites yield comparable transient electronic responses and device performance to their "hybrid" relatives (64).

2.2.2. Organic cation dynamics. Hybrid halide perovskites are plastic crystals, and the dynamically disordered organic cations impart new degrees of freedom relative to conventional compound semiconductors. These dynamics play a role in various functional properties, deriving primarily from their polarizability (65). Nearly half of the static dielectric polarizability of $CH_3NH_3PbI_3$ derives from the dynamic molecules, akin to that of a polar solvent such as water (**Figure 2e,f**). This polarizability has several implications for charge transport, summarized in **Figure 1c** and described below.

Although the exact mechanism behind the long excited-state lifetimes for thermalized and hot carriers remains debated, the orientational dynamics of the organic molecules play an important role in many (and not mutually exclusive) hypotheses. Organic cation dynamics have been implicated in the formation of large polarons that interact with both exciton (66) and free charge carriers (67, 68). The presence of dynamic organic cations accelerates the polaron formation

Fröhlich interaction: coupling of a charge to the presence of the electric field generated from a longitudinal optical phonon

Lone-pair electrons: The ns^2 valence electrons on B can be stereochemically activated to create space-filling lone-pair electrons similar to those of NH_3

Plastic crystals: characterized by a lack of orientational order with preservation of translational order
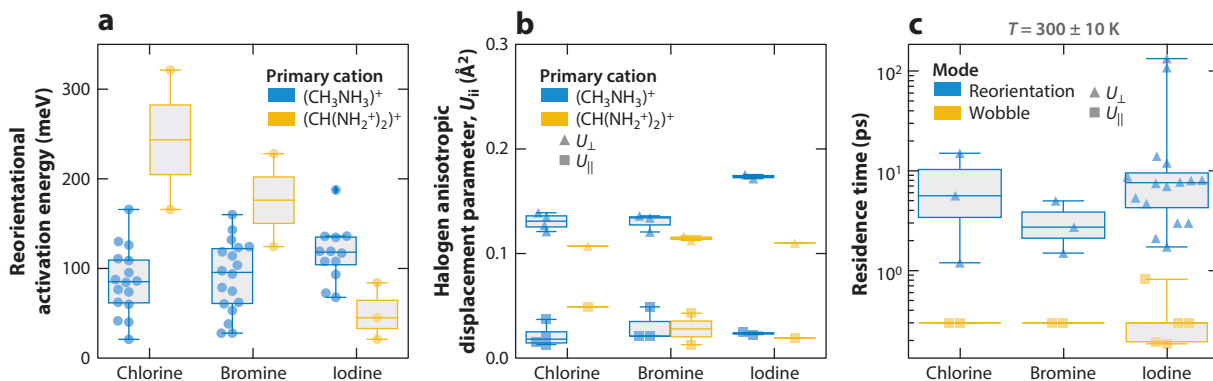
Figure 3

Distribution of activation energies and residence times for organic cation dynamics in $APbX_3$ phases, as differentiated by halogen (A = methylammonium, formamidinium; X = Cl, Br, I). (*a*) Activation energies for molecular reorientational motion further differentiated by organic cation, illustrated by box plots and swarms of individual data points. (*b*) Anisotropic displacement parameters (ADPs) of halogen positions in cubic unit cells (Pm$\bar{3}$m) further differentiated by organic cation, illustrated by box plots and swarms of individual data points. The ADPs are separated into those perpendicular to ($U_\perp$) and parallel to ($U_\parallel$) the Pb–X bonds. (*c*) Residence times at $T = 300 \pm 10$ K for either reorientational (e.g., whole-molecule tumble) or wobble (e.g., C_3 rotation about a C–N axis in methylammonium) motions, including methylammonium- and formamidinium-based phases in their tetragonal and cubic phases. Box plots illustrate the median (*horizontal lines*) and mean (*box center*), while the markers illustrate data points. Data compiled from multiple references are tabulated in the Supplemental Material (39, 47, 51, 53, 73–85).

time [0.3 ps in $CH_3NH_3PbBr_3$ versus 0.7 ps in $CsPbBr_3$ (69)], which extends the lifetime of hot carriers (70). The coupling of inorganic lattice distortions and organic cation reorientations has been shown to screen charge carriers and excitons (13, 14). For example, the lack of interactions between independently reorienting molecules yields a low vibrational group velocity and, thus, poor thermal conductivity with a high heat capacity—an ideal recipe for a phonon bottleneck, in which energetic carriers cannot thermalize efficiently with the lattice due to poor heat removal, as detected by pump-probe spectroscopy experiments (19, 71, 72) and supported by a polaron model backed by density functional theory calculations (68).

Furthermore, the presence of polar fluctuations has the potential to locally and transiently break inversion symmetry of the bulk crystal. Given the slow orientational timescale of the organic dynamics (∼5–15 ps) (**Figure 3**) relative to electronic dynamics, it has been proposed that Rashba spin-split valence bands can give rise to direct bandgap-like efficient optical absorption transitions (21, 86–88); carrier thermalization leads to shifted momenta, resulting in indirect-like recombination and longer lifetimes (**Figure 1c**). Experiments have concluded that the halide perovskites can support static (89, 90) and dynamic (91–94) Rashba spin splitting, with recent evidence that the static effect persists only at low temperatures in hybrids and that both all-inorganic and hybrid materials host a dynamic Rashba effect at room temperature (95). The dynamic Rashba effect appears to originate from anharmonic, polar thermal fluctuations of the inorganic octahedra that may arise from lone-pair electron activity and their interactions with organic cation reorientations or cesium motions (61–63, 95). Therefore, the interplay between organic- and inorganic-centered dynamics has the potential to influence the electronic excited-state dynamics.

The dynamic organic molecules also influence ionic transport and diffusion. Hybrid halide perovskites have a significant ionic contribution to conductivity under various circumstances (23, 25, 96, 97), including under light illumination (24). While ion motion leads to device hysteresis (23), phase separation (98), and decomposition (24), motion of the halogens can lead to the creation

of short-lived electronic defects. Such rapid defect creation can result in defect densities above the thermodynamic limit with sufficiently short lifetimes as to be benign to carrier scattering (99), a finding that is further supported by the self-elimination of intrinsic defects on cooling (100). Furthermore, the timescale of defect motion is faster in hybrid perovskites, as illustrated by the relatively fast self-healing of $CH_3NH_3PbBr_3$ and $CH(NH_2)_2PbBr_3$ from laser-induced defects relative to $CsPbBr_3$ (22). While this fast self-healing leads to a high tolerance for unintentional defects, it makes controlled doping very challenging.

Given the importance of reorientational dynamics in hybrid perovskites for their functional performance, many studies have sought to understand the nature of these dynamics, both of simple hybrid halide perovskites and of technologically relevant complex alloys (101). The remainder of this review describes several case studies of organic cation dynamics through neutron scattering and complementary techniques.

3. CASE STUDIES OF HYBRID PEROVSKITE SEMICONDUCTORS

Myriad competing interactions govern the complex dynamics in hybrid perovskites. The activation energies and residence times of the reorientations of organic cations for several $APbX_3$ perovskites shown in **Figure 3** reflect several trends in ionic size and hydrogen bonding strength. In phases where reorientational dynamics are present (e.g., tetragonal and cubic) (**Figure 3a**), the activation energy of that motion shows distinct trends for each organic cation. In methylammonium perovskites, the activation energy stays relatively constant as a function of halogen, which correlates more strongly with the constant energy of hydrogen bonding across the halogen series (0.26–0.27 eV/cell) (102) than with the changing size of the halogen (**Figure 1**). However, the nature of the halogen does influence the reorientational barrier in formamidinium perovskites, where the increasing size of the halogen leads to an increased cuboctahedral void size to allow for less inhibited molecular reorientations. This also follows the expected trend in hydrogen bonding strength: 0.16 eV/cell for chlorine, 0.1 eV/cell for bromine, and 0.09 eV/cell for iodine (102). The smaller size of methylammonium decreases the importance of the cuboctahedral void size; the stronger dipole moment of methylammonium yields a higher contribution of hydrogen bonding to the total energy (102). However, the activation energy for methylammonium reorientations increases for iodine, which correlates with an increase in the crystallographic atomic displacement parameter of iodide perpendicular to the Pb–X bond that dynamically decreases the cuboctahedral void size (**Figure 3b**).

Additional complexity is apparent upon examination of the residence times of organic molecules. For both methylammonium and formamidinium perovskites, studies reveal two characteristic residence times for two distinct motions identified as a long-timescale reorientation and a short-timescale wobble (∼17 ps and ∼0.33 ps, respectively) (**Figure 3c**). These data demonstrate the composition-dependent interplay of hydrogen bonding and steric interactions on each reorientational mode.

In this section, we present case studies of organic cation dynamics based on neutron spectroscopy and complementary techniques [e.g., nuclear magnetic resonance (NMR), dielectric spectroscopy, time-resolved vibrational spectroscopy], as well as their dependence on chemical substitution and their relationships with optoelectronic properties. These case studies demonstrate the insight that neutron scattering has to offer for hybrid halide perovskites.

3.1. Unsubstituted Hybrid Halide Perovskites

Methylammonium and formamidinium lead halide perovskites are the archetypal members of this family and present complex dynamics essential to understanding substituted materials found in applications and devices.
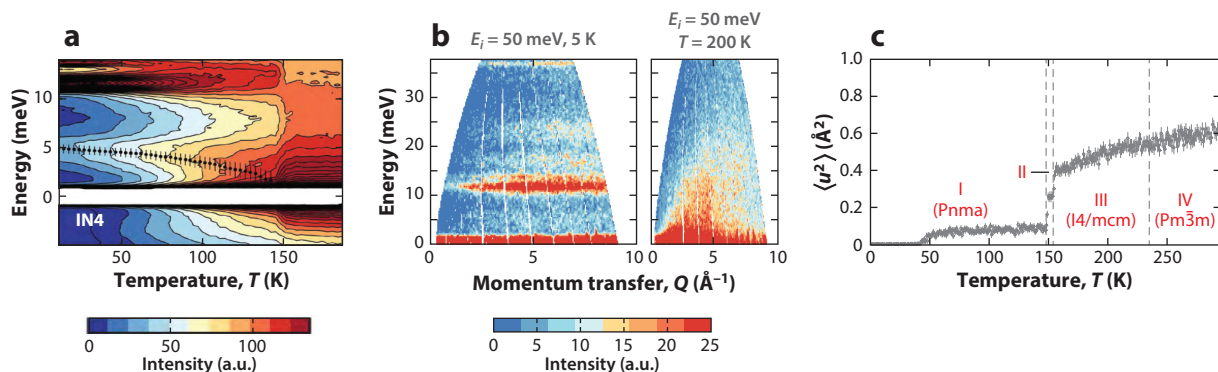
Figure 4

(*a*) Inelastic neutron scattering (*Q* integrated and powder averaged) collected on the IN4 spectrometer from $CH_3NH_3PbBr_3$, showing softening of an ~5-meV phonon as well as the replacement of an ~11-meV vibrational mode with a broad, quasi-elastic relaxation above the orthorhombic-to-tetragonal phase transition. (*b*) Inelastic neutron scattering as $S(Q, \omega)$ from powder $CH_3NH_3PbBr_3$, showing the significant overdamping of modes at $T = 200$ K. The sharp, harmonic modes are replaced by quasi-elastic fluctuations extending up to high energies. (*c*) Mean squared displacement of $CH_3NH_3PbBr_3$, $\langle u^2 \rangle$, extracted from an elastic window scan as a function of temperature, showing significant changes in hydrogen dynamics at the tetragonal-to-orthorhombic phase transition, as well as below $T \approx 50$ K. Figure adapted with permission from Reference 47, copyright 2015 American Physical Society.

3.1.1. Methylammonium lead halide perovskites.

Methylammonium lead halide perovskites have been the archetypal hybrid perovskite for solar applications, due to the advantageous bandgap of methylammonium lead iodide and the ease of preparation of methylammonium lead iodide compared with the cesium and formamidinium analogs (2, 103, 104). Early NMR and calorimetric studies demonstrated that methylammonium is dynamically disordered in the high-temperature cubic phase, with increased orientational ordering on cooling that relates to the two known phase transitions (105). Between 400 K and 100 K, methylammonium lead iodide transitions from the high-temperature cubic phase (space group: Pm$\bar{3}$m) to a tetragonal phase (space group: I4/mcm) characterized by out-of-phase octahedral rotations when looking perpendicular to the *c* axis (Glazer notation: $a^0a^0c^-$), and then to an orthorhombic phase (space group: Pnma) characterized by additional octahedral tilt axes (Glazer notation: $a^-b^+a^-$) (105). These transitions change the shape and size of the cuboctahedral void where methylammonium sits and, thus, its dynamical behavior.

The phase behavior of $CH_3NH_3PbX_3$ perovskites reflects the presence of organic–inorganic coupling. The phonon dispersion measured in the cubic phase of methylammonium lead iodide with high-energy resolution inelastic X-ray scattering revealed large-amplitude and anharmonic zone-edge rotational instabilities of the octahedra and short-range disorder of the octahedra (48). This disorder is largest for the hybrids, as opposed to all-inorganic materials (106). Subsequent neutron scattering revealed that these instabilities are resolution limited in energy, and thus correspond to static (i.e., with lifetime of $\tau > 36$ ps) tetragonal domains similar to the critical scattering observed from SrTiO₃ (49). First-principles calculations reveal that these instabilities are strongly coupled to the librations and reorientations of methylammonium (48).

In $CH_3NH_3PbBr_3$, there is a clear correlation between the phonons of the lead bromide framework and methylammonium dynamics. At the orthorhombic-to-tetragonal order–disorder transition, sharp modes attributed to methylammonium vibrations decrease in scattered amplitude while heating; at the transition these modes are replaced by broad QENS associated with methylammonium reorientation (**Figure 4a**). The decrease in vibrational mode scattering amplitude accompanies the softening of an ~5-meV optical phonon from the lead bromide

framework. Furthermore, the tetragonal-phase phonons become strongly overdamped when the organic cations become significantly dynamic (**Figure 4b**). In $CH_3NH_3PbCl_3$, one observes overdamping of the framework phonon modes across the same temperature scale, as observed with bromine, but without the order–disorder phase transition (107).

Given the significance of hydrogen bonding in $CH_3NH_3PbX_3$ (102), the organic–inorganic interactions are a likely source of anharmonic behavior, as supported by density functional theory calculations of the rotational energy barriers (81). Organic–inorganic coupling in the form of so-called nodding donkey modes are observed in Raman and IR spectroscopy experiments and density functional theory–based calculations thereof (108, 109). The vacancy-ordered double perovskites that lack covalent connectivity between octahedra [e.g., $(CH_3NH_3)_2SnI_6$] also show anharmonic tilting behavior that is correlated with the presence of organic cations (110). Understanding this anharmonicity, and its origins in the organic cation dynamics, is important for describing locally broken symmetries as well as the nature of electron–phonon coupling beyond the linear response (111).

Methylammonium rapidly reorients in the high-temperature cubic phase and exhibits a decrease in amplitude, timescale, and dynamic degrees of freedom on cooling as the cuboctahedral void constricts, as demonstrated by extensive neutron scattering and complementary NMR spectroscopy studies. In methylammonium lead bromide, the temperature-dependent MSDs calculated from incoherent elastic neutron scattering (47) (**Figure 4c**) capture the overall decrease in motion. The lack of anomalies in $\langle u^2 \rangle$ at the cubic-to-tetragonal phase transition suggests that the entropy loss associated with this phase transition [8.2 J/(mol·K), $\approx R\ln(2.7)$ (51)] correlates to a change in the type of motion rather than to a reduction in the spatial extent of methylammonium dynamics, $\langle u^2 \rangle$. In contrast, the clear feature in the MSD at the tetragonal-to-orthorhombic phase transition suggests a discontinuous change in how methylammonium reorients in the cuboctahedral void. These observations are also consistent with the conservation of ^1H and ^{14}N NMR line shapes across the cubic-to-tetragonal phase transition and appreciable narrowing after the tetragonal-to-orthorhombic phase transition (74, 82).

The reorientational dynamics of methylammonium are well described by a jump model of transitions between idealized orientations, as originally suggested by changes in degrees of freedom at various phase transitions determined from calorimetry (51). A rigorous group theoretical analysis by Chen et al. (73) with a jump model provided a complete description of the QENS data (**Figure 5**). This jump model involves the direct product of a C_3 rotation (120°) derived from the internal symmetry axis of methylammonium and a C_4 rotation (90°) perpendicular to the C_3 rotation as imposed by the symmetry of the lattice site point group symmetry. Both the C_3 and C_4 modes are active in the cubic and tetragonal phases, with relaxation times of ~1 ps and ~5 ps, respectively, as determined by two different studies (73, 80). This analysis of the QENS is consistent with direct measurements of the molecular dynamics; two-dimensional transient IR spectroscopy also reveals the presence of a fast (300-fs) wobbling-in-a-cone motion similar to the C_3 rotation and a slow (3-ps) molecular reorientation similar to the C_4 rotation (39).

The molecular reorientations correlate most strongly to the dielectric response. As shown in **Figure 5b**, the C_4 motion increases significantly in relaxation time on cooling within the tetragonal phase, but this reorientation is frozen out upon cooling into the orthorhombic phase. Therefore, loss of the C_4 reorientation leads to a significant decrease in the dielectric function (41, 53, 105, 112, 113), schematically depicted in **Figure 2**.

Through this organic–inorganic coupling, the dynamic degrees of freedom of methylammonium correlate with changes in the optoelectronic properties. For example, the freezing out of the C_4 whole molecular reorientation at the tetragonal-to-orthorhombic phase transition correlates with faster recombination of excited-state charge carriers as well as with an increase in exciton
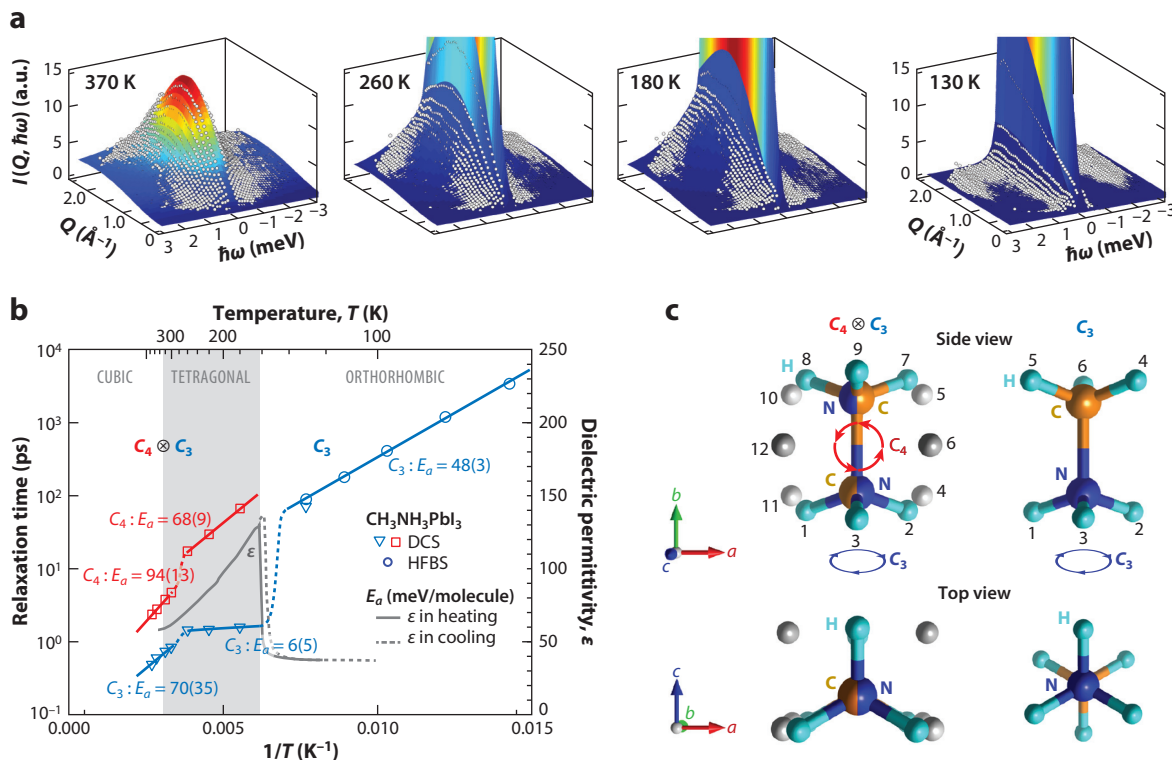
Figure 5

(*a*) Quasi-elastic neutron scattering (QENS) from $CH_3NH_3PbI_3$. Neutron scattering intensity is shown as a function of momentum (Q) and energy ($\hbar\omega$) transfers, measured at 370 K, 260 K, 180 K, and 130 K. Open circles represent the data, and the color-coded surface is the surface image of the calculated jump model. (*b*) Relaxation time, τ, of rotational modes of $CH_3NH_3PbI_3$ obtained from fitting QENS data at various temperatures and plotting them against inverse temperature ($1/T$). The colored solid lines represent the fits to $\ln(\tau) = E_a/(k_B T) - \ln(A)$, where E_a is an activation energy in units of meV per molecule, k_B is the Boltzmann constant, and A is a preexponential factor. The colored dotted lines are guides for the eye. The gray solid and dotted lines represent temperature-dependent dielectric permittivity measured at 1 kHz by Onoda-Yamamuro et al. (53), showing a sharp increase at 160 K. (*c*) $C_3 \otimes C_4$: 12 crystallographically equivalent sites for H atoms of $CH_3NH_3^+$ in the tetragonal environment. C_3: 3 equivalent H atomic sites in the orthorhombic environment. Abbreviations: DCS, disc chopper spectrometer; HFBS, high-flux backscattering spectrometer. Figure adapted with permission from Reference 73, copyright 2015 Royal Society of Chemistry.

binding energies (114, 115). These correlations suggest that the methylammonium C_4 reorientations participate in the electron–phonon models depicted in **Figure 1**.

3.1.2. Formamidinium lead halide perovskites. Formamidinium lead halide perovskites typically have unusual phase behavior in comparison to methylammonium and cesium analogs, including reentrant phase transitions (116), path-dependent phase transitions (104), and crystallographically unresolvable phase transitions (76). Similar to methylammonium perovskites, formamidinium lead halide perovskites exhibit dynamic degrees of freedom within the organic sublattice that freeze out with temperature, which is reflected in the temperature dependence of the dielectric permittivity (75, 76, 113, 116). Anomalies in the temperature-dependent permittivity also occur at phase transition temperatures. Despite these similarities with methylammonium perovskites, the distinct molecular shape and delocalized cationic π system yield several distinctions in formamidinium perovskites.
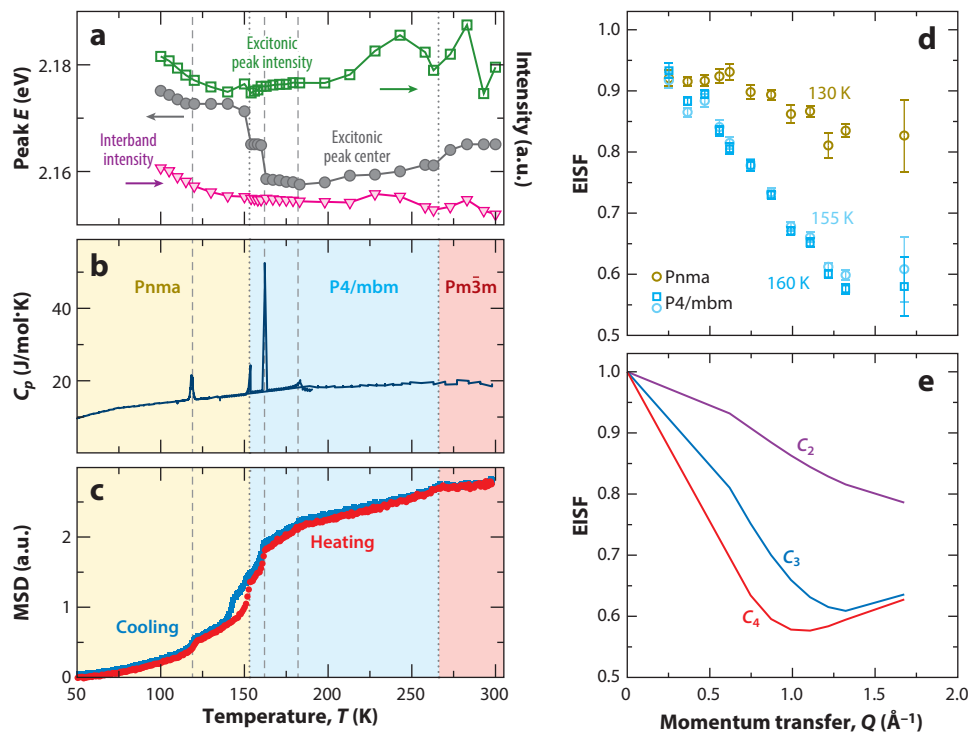
Figure 6

(*a*) Parameters from modeling the temperature-dependent photoconductivity of $CH(NH_2)_2PbBr_3$. Excitonic peak center (*left axis*, *gray circles*), excitonic peak intensity (*right axis*, *green squares*), and interband intensity (*right axis*, *pink triangles*). (*b*) Heat capacity data for $CH(NH_2)_2PbBr_3$. The crystallographically observed phase transitions occur at 266 K and 153 K. (*c*) Mean squared displacements (MSDs) determined from fixed-window elastic neutron scattering of $CH(NH_2)_2PbBr_3$ measured on heating (*red circles*) and cooling (*blue squares*). The colored rectangular overlays in panels *b* and *c* illustrate the crystallographic symmetry at each temperature, with dotted gray lines indicating the crystallographic phase transition temperatures and dashed gray lines showing other phase transition temperatures determined from heat capacity and differential scanning calorimetry data. (*d*) Elastic incoherent structure factors (EISFs) extracted from quasi-elastic neutron scattering spectra at $T = 160$ K, 155 K, and 130 K. (*e*) Models of C_2, C_3, and C_4 molecular rotations shown for comparison. Figure adapted with permission from Reference 76, copyright 2019 American Chemical Society.

Formamidinium lead bromide is notable for having five temperature-dependent anomalies in the MSDs that correlate with anomalies in heat capacity and photoconductivity (76) (**Figure 6**), as well as thermal expansion from dilatometry (117). Two of these phase transitions correspond to changes in crystallographic symmetry, with detectable changes in the octahedral tilting and rotation patterns (76, 118). The remaining three phase transitions release entropy but do not correlate with a readily detectable change in crystallographic symmetry (76, 78, 117). Instead, they are characterized by changes in the dynamic degrees of freedom of formamidinium. As of early 2021, these crystallographically unresolvable phase transitions are unique among hybrid perovskites, although formamidinium lead iodide shows unusual, sample history–dependent phase transitions that are either reentrant and/or entropy stabilized (104, 116).

Based on the molecular geometry, the natural rotations for formamidinium are 180° rotations with the axis of rotation parallel to the carbon–hydrogen bond or about the axis connecting the two nitrogen atoms, as well as a 120° rotation orthogonal to the molecular plane (**Figure 1a**).

The point group symmetry of the ideal lattice site occupied by formamidinium suggests that the molecule could undergo reorientational C_4 rotations. Molecular dynamics simulations and density functional theory calculations predict that C_2 rotations, where the axis of rotation connects the two nitrogen atoms rather than a higher symmetry location, are the lowest-energy molecular dynamics (75, 119); these simulations also suggest the presence of a slow reorientation and a fast reorientation, in analogy to those observed in methylammonium perovskites (119). However, direct modeling of the experimental inelastic coherent structure factor is complicated by the complex orientational potential energy landscape of formamidinium within the nearly cuboctahedral void. The EISF resembles a motion between idealized C_3 (120°) and C_4 (90°) rotations at elevated temperatures but 180° rotation at lower temperatures (**Figure 6e**), consistent with changes in the relaxation times marked by the reduction in QENS peak width across phase transitions (76).

The complex behavior of formamidinium dynamics appears to be related to its distinct distribution of electrostatic charges. Formamidinium has a weaker dipole moment and stronger quadrupole moment than methylammonium (120). A pair of molecular quadrupoles embedded in a dielectric crystal prefer to orient perpendicular to each other in a T shape (121), which can couple strongly to compressive and expansive strains from the surrounding anionic lattice (78). This pairwise T shape cannot tile on any Bravais lattice; therefore, the molecular orientations of formamidinium are frustrated (76). Frustrated orientations are consistent with NMR results showing that formamidinium reorients more quickly than methylammonium and with dielectric susceptibility measurements that indicate a series of complex changes in formamidinium dynamics at low temperatures (118, 122). This geometric frustration participates in the orientational phase transitions of formamidinium lead bromide observed with QENS and could explain the path-dependent phase transitions of formamidinium lead iodide. [79]Br nuclear quadrupolar resonance (NQR) data suggest that the reorientations of formamidinium couple to changes in the local environment around the inorganic octahedra, aligning with first-principles calculations showing that the rotational energy barrier of formamidinium can be tuned with substitution on the halide and metal sites (78, 123). Understanding the unusual phase behavior of formamidinium perovskites is essential to understanding their properties, as each phase has a different optoelectronic behavior (76, 116).

3.1.3. Lead-free hybrid halide perovskites.

While more difficult to experimentally study (e.g., due to air sensitivity), tin and germanium perovskites offer new opportunities for functional properties, as they show an increased contribution from ns^2 lone-pair electrons and lack the toxicity of lead (57, 124, 125). The increased stereochemical activity in tin and germanium perovskites relative to that in lead perovskites (106, 126) is expected to couple to the dynamic degrees of freedom of methylammonium (58), although studies so far have focused predominantly on ionic conductivity (127, 128). However, density functional theory calculations also indicate that tin and germanium perovskites have higher energy barriers for methylammonium reorientations, attributed to a decrease in lattice polarizability and compression of the A-site void (81, 129, 130). Furthermore, the overall phase behavior appears to be more sensitive to the molecular dynamics, as isotope enrichment can completely change [e.g., $CH_3NH_3SnBr_3$ (131) versus $CD_3ND_3SnBr_3$ (54)] or suppress phase transitions [e.g., $CH_3NH_3GeCl_3$ versus $CD_3ND_3GeCl_3$ (128)]. Experimental validation of these computational predictions and investigation into lone-pair coupling to methylammonium dynamic degrees of freedom provide exciting avenues for continued research.

3.2. Effects of Chemical Substitution

Most of the technologically relevant hybrid halide perovskites for photovoltaic applications are heavily chemically substituted (i.e., alloyed), as exemplified by a high-performing composition:

$(CH(NH_2)_2)_{0.79}(CH_3NH_3)_{0.16}Cs_{0.05}Pb(I_{0.84}Br_{0.17})_3$ (101). Chemical substitution is easily accomplished synthetically in the solution-phase or solid-state route to these materials (101, 132), which enables tuning of optoelectronic properties such as the bandgap and polaron mobility (27, 133). Furthermore, the unsubstituted hybrid perovskites methylammonium lead iodide and formamidinium lead iodide are enthalpically unstable (29) and decompose rapidly under ambient conditions (134–137); certain substitutions stabilize the perovskite phases (138) or slow this decomposition process (101, 139, 140). While chemical substitution can improve phase stability, it modifies the internal energy landscape of hybrid perovskites, which influences the atomistic dynamics and, thus, electron–phonon coupling (27, 141).

This section focuses on the role of cesium substitution in the two perovskite materials described above, methylammonium lead bromide and formamidinium lead bromide. In contrast to the hybrid materials, cesium lead bromide exhibits orthorhombic symmetry with octahedral tilting at and below room temperature, with the cubic and tetragonal phases accessible at temperatures above 80°C and 140°C, respectively (142). The generalized phase behavior of the substituted alloys can be understood within the context of a pseudobinary phase diagram, where compositions closest to the end members behave as solid solutions separated by a two-phase region for intermediate compositions. However, the detailed nature of the phase transitions requires closer examination of the dynamic nature of the organic cations in these plastic crystals.

3.2.1. Cesium substitution in methylammonium lead bromide.

In methylammonium lead bromide, cesium substitution for methylammonium leads to inhibition of the methylammonium dynamics. As discussed above, methylammonium undergoes 90° rotations perpendicular and 120° rotations parallel to the carbon–nitrogen bond axis (73). Substitution of cesium for methylammonium in the solid solution, $(CH_3NH_3)_{1-x}Cs_xPbBr_3$, does not affect the identity of these rotations; however, modeling of the QENS spectra demonstrates that a fraction of molecules become pinned as the concentration of cesium increases (77) (**Figure 7a–c**). As discussed above, the molecular reorientations are directly responsible for a significant fraction of the increased dielectric polarizability (**Figure 5b**).

The pinning of molecular reorientations with a cesium substitution in $(CH_3NH_3)_{1-x}Cs_xPbBr_3$ correlates with a significant modification of the phase behavior. In contrast to $CH_3NH_3PbBr_3$ (**Figure 4**), the temperature-dependent MSDs vary smoothly with temperature and do not show abrupt changes near crystallographic phase transition temperatures in the substituted materials (77) (**Figure 7**). Crystallography indicates that, with increasing substitution, the phase transitions occur over a wider temperature range and are dependent on temperature ramp rate (77). The sluggish phase transitions and inhibited dynamics indicate that methylammonium lead bromide becomes an orientational glass upon cesium substitution characterized by disordered and frozen methylammonium orientations, similar to bromide substitution in potassium cyanide (59).

In analogy to spin glasses, the formation of an orientational glass involves frustration of order parameters related to the orientation of the molecule (59). A possible reason for the increased frustration on substitution is that cesium and methylammonium prefer different coordination within the octahedral framework. Most halide perovskites crystallize in the tetragonal P4/mbm phase, characterized by in-phase octahedral rotations, as this configuration maximizes *A*-site coordination (143). Hydrogen bonding interactions between methylammonium and the octahedral framework cause methylammonium perovskites to prefer the tetragonal I4/mcm phase, characterized by out-of-phase octahedral rotations (144–146). These interactions, combined with the contraction of the *A* site with cesium substitution, compete and lead to the inhibition of methylammonium reorientations and the formation of an orientational glass. It appears that substitution increases
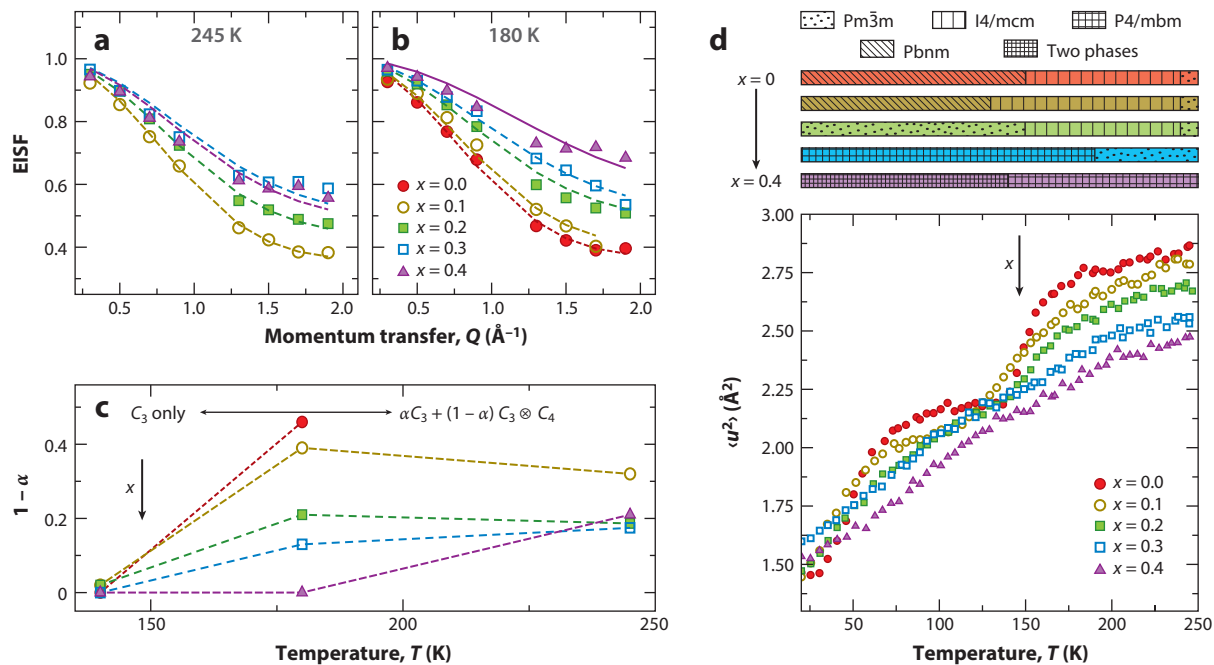
Figure 7

Selected elastic incoherent structure factor (EISF) values for $(CH_3NH_3)_{1-x}Cs_xPbBr_3$ extracted from quasi-elastic neutron scattering (QENS) spectra collected at (*a*) 245 K and (*b*) 180 K. The dashed lines represent fits to the coupled C_3 and C_4 jump model, and the solid lines represent fits to the C_3 jump model. (*c*) The fraction of $CH_3NH_3^+$ participating in a $C_3 \otimes C_4$ rotation $(1 - \alpha)$ from the EISF modeling. The dashed lines are guides for the eye. (*d*) Mean squared displacements as a function of temperature extracted from QENS spectra of $(CH_3NH_3)_{1-x}Cs_xPbBr_3$, illustrating a smearing of transitions with increasing x. The bars at the top illustrate the observed lattice symmetry of $(CH_3NH_3)_{1-x}Cs_xPbBr_3$ for $x = 0.0$, 0.1, 0.2, 0.3, and 0.4. Figure adapted with permission from Reference 77, copyright 2017 American Chemical Society.

the influence of hydrogen bonding (cf. **Figure 3**). Recent first-principles calculations suggest that reductions in symmetry, such as those from frozen or inhibited methylammonium reorientations, change the binding energy of polarons (27) or tune the magnitude of Rashba splitting (141), indicating that substitution influences electronic properties through organic cation dynamics.

3.2.2. Cesium substitution in formamidinium lead bromide. The orientational phase transitions of formamidinium lead bromide are sensitive to chemical substitution. The five phase transitions of formamidinium lead bromide have dynamic signatures that manifest in ${}^1H$ NMR, ${}^{14}N$ NMR, and MSDs between room temperature and 100 K (**Figure 6**). However, formamidinium lead bromide substituted with as little as 5–10% cesium exhibits only one anomaly in ${}^1H$ NMR, ${}^{14}N$ NMR, or MSDs between room temperature and 100 K, which corresponds to the high-temperature cubic-to-tetragonal phase transition (78) (**Figure 8*a***).

Cesium substitution effectively suppresses the four low-temperature phase transitions by interrupting the concerted changes in formamidinium dynamics. At room temperature, ${}^{14}N$ NMR spectra of $(CH(NH_2)_2)_{1-x}Cs_xPbBr_3$ show retained reorientational dynamics, but with an increased anisotropy of the ${}^{14}N$ environment with *x*; the anisotropy accompanies a clear distortion of the local ${}^{79}Br$ environments, as determined by NQR spectroscopy (**Figure 8*b***). The interplay between substitution and formamidinium orientation reflects a behavior distinct from that of methylammonium (**Figure 3**), which can be linked to the large electrostatic quadrupolar
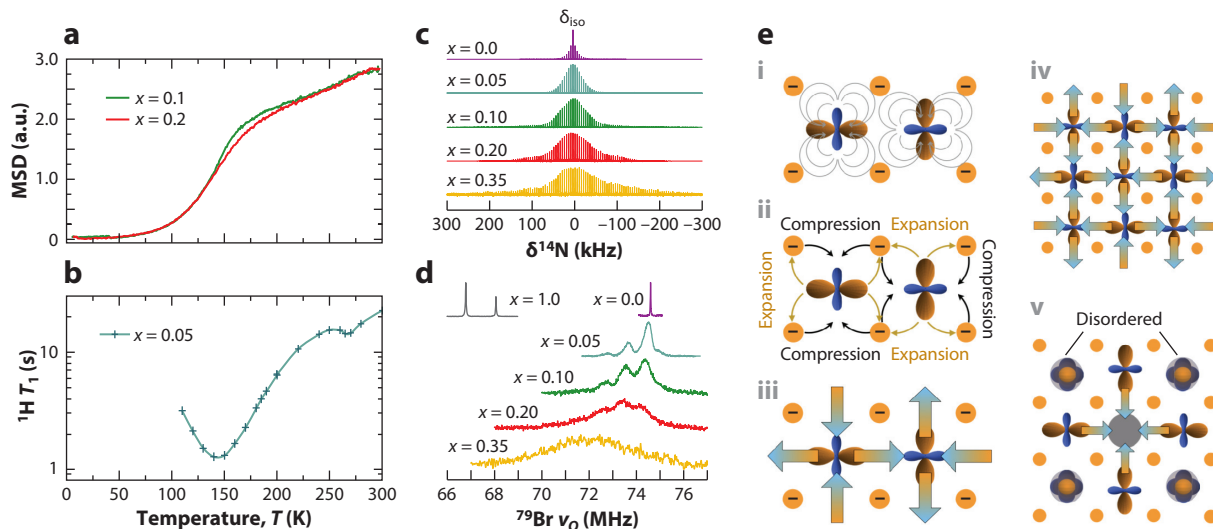
Figure 8

(*a*) Mean squared displacements (MSDs) extracted from fixed-window elastic neutron scattering spectra for $(CH(NH_2)_2)_{1-x}Cs_xPbBr_3$, where $x = 0.1$ and 0.2, illustrate a lack of discontinuities in substituted samples (in contrast to **Figure 6c**). (*b*) Spin-lattice relaxation time (T_1) determined from ^1H NMR spectroscopy of $(CH(NH_2)_2)_{0.95}Cs_{0.05}PbBr_3$ illustrates one phase transition at $T \sim 260$ K. (*c*) Room-temperature ^{14}N NMR spectra of $(CH(NH_2)_2)_{1-x}Cs_xPbBr_3$, where $x = 0$ to 0.35, illustrate an increased anisotropy of cation rotations with x. (*d*) Room-temperature ^{79}Br NQR spectra collected for $(CH(NH_2)_2)_{1-x}Cs_xPbBr_3$ show that increasing the level of substitution leads to an effectively continuous distribution of possible local environments. (*e*) (*i, ii*) Electrostatic potential field lines emanating from the quadrupolar moment of formamidinium (*orange* denotes negative density; *blue* denotes positive density) yield attractive or repulsive interactions to the anionic framework. (*iii*) The resulting expansive and compressive strain fields map onto an elastic dipole tensor (*large arrows*). (*iv*) In a plane, the elastic dipoles can order; however, a favorable three-dimensional configuration cannot be tiled. (*v*) The smaller Cs^+ cation introduces compressive local strain, thereby causing a preferred orientation of quadrupolar cations around the Cs^+ and frustrated orientations of the next-nearest-neighboring quadrupoles. Figure adapted with permission from Reference 78, copyright 2020 American Chemical Society.

moment of formamidinium (**Figure 8c**). The relative orientations of formamidinium within the inorganic framework are mediated by the electrostatic quadrupolar field, which is very sensitive to the surrounding electric field gradient. When this interaction is mapped onto an elastic dipole tensor, one can see how a stable long-range-ordered configuration becomes challenging to produce (i.e., it is frustrated). Introduction of compressive microstrain from the smaller cesium cation significantly changes the potential energy landscape, with consequences for the long-range order and phase transitions (78). While the long-range order is strongly influenced by the substitution, the local dynamics of formamidinium appear to be mostly retained (78), suggesting that formamidinium-based perovskites serve as a better host for substituted alloys if one wishes to maintain a larger dielectric response.

3.2.3. Complex, multiple substitutions in hybrid halide perovskites.

The ability to use a cocktail of cations and anions to create highly stable, functional photovoltaic devices reflects a unique defect tolerance of hybrid perovskites (101). While pseudobinary solid solutions formed by substitution on either the A site [e.g., $(CH(NH_2)_2)_{1-x}Cs_xPbI_3$ (147)] or the halogen site [e.g., $CH_3NH_3Pb(I_{1-x}Br_x)_3$ (98)] are prone to phase separation and decomposition, complex, multiple substitutions on both A and halogen sites prevent this phase separation (148). The chemical pressure from cesium substitution for methylammonium in $(CH_3NH_3)_{0.5}Cs_{0.5}Pb(Br_{0.5}I_{0.5})_3$ appears

to have the same influence as exerting 0.2 GPa of external pressure on $CH_3NH_3Pb(Br_{0.5}I_{0.5})_3$ and thermodynamically stabilizes the solid solution, highlighting the importance of an often-overlooked $P\Delta V$ term in the thermodynamic potential (149).

Therefore, one expects complex substitutions to also influence the organic molecular dynamics. The inhibition with cesium substitution in methylammonium perovskites resembles that of methylammonium-substituted formamidinium lead iodide, in which line-shape analysis of ^{14}N NMR spectra reveals that methylammonium and formamidinium reorientations become increasingly anisotropic with increased substitution (122). Substitution at the halide site, as has been used to increase stability and tune the electronic bandgap (101, 150), also leads to inhibited cation dynamics. Pump-probe two-dimensional IR spectroscopy studies of $CH_3NH_3Pb(Cl_xBr_{1-x})_3$ and $CH_3NH_3Pb(Br_xI_{1-x})_3$ show that both series exhibit slower methylammonium dynamics than either end member (79). This finding supports the observation of decreased orientational disorder in methylammonium lead bromide after chlorine substitution, as determined by Fourier difference maps from Rietveld refinement of neutron powder diffraction (151). Many of the top-performing photovoltaic devices substitute a formamidinium-based host (1). Given that local formamidinium dynamics are not significantly inhibited by substitution (78), any advantage of having a dynamic organic cation is still active in formamidinium-based materials.

4. CONCLUSIONS AND OUTLOOK

Collective and local dynamics in hybrid perovskites underlie the optoelectronic properties that make them of interest for photovoltaics, radiation detection, and light-emitting diodes. Therefore, characterization of these dynamics is essential for building useful theories to describe their behavior, especially for local dynamics that do not yet have rigorous models. Neutron scattering plays a large role in uncovering these dynamics—the dynamic structure factor, $S(Q, \omega)$, informs researchers of the correlations of these molecular dynamics in both space and time. Complementary methods, such as NMR, dielectric spectroscopies, X-ray scattering, molecular dynamics simulations, and density functional theory calculations, provide a complete perspective across many environmental conditions. Neutron scattering has been used to track changes in molecular dynamics as a function of temperature, to describe the symmetry of molecular reorientations, and to characterize the activation energy of molecular dynamics. These investigations demonstrate that these local dynamics are affected by cation identity, by electrostatic and hydrogen bonding interactions with the extended octahedral framework, and by substitution. This relationship creates a deeper understanding of the phase behavior of hybrid halide perovskites. Investigations into two-dimensional perovskite materials have only just begun, and many questions remain about the dynamic degrees of freedom of bulky organic cations and their relationship to optoelectronic properties. Similar questions remain for other hybrid perovskite derivatives, including zero-dimensional vacancy-ordered perovskites. These insights are the basis of rigorous structure–property relationships that will enable innovations in next-generation semiconductors.

SUMMARY POINTS

1. Hybrid perovskite semiconductors are plastic crystals with dynamically reorienting organic cations.
2. Organic cation dynamics have a direct influence on the dielectric response of hybrid perovskite semiconductors.

3. Molecular reorientational dynamics exert indirect influences on the optical and electronic properties of hybrid perovskites by way of locally broken symmetry, electron–phonon coupling, and defect creation and motion.

4. Chemical substitution of hybrid perovskite semiconductors influences the thermodynamic stability and dynamics of organic cations.

DISCLOSURE STATEMENT

The authors are not aware of any affiliations, memberships, funding, or financial holdings that might be perceived as affecting the objectivity of this review.

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